



APPLICATION OF THE METHOD OF INDETERMINATE LAGRANGE MULTIPLIERS FOR OPTIMAL POWER DISTRIBUTION OF COMPENSATING DEVICES BETWEEN CONSUMERS

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Article history:	Abstract:
Received: 10 th November 2022	This article discusses the calculations of determining the optimal value of the reactive power among consumers in terms of the lowest costs and compensation for active power losses using Excel. The most optimal option is to calculate by coordinates, and the results obtained using nonlinear programming methods are compared with each other.
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INTRODUCTION. In the production of electricity at power plants and consumption in the national economy of Uzbekistan, special attention is paid to improving its quality and rational use.

Optimization is usually understood as a purposeful activity, which consists in obtaining the best results under appropriate conditions. The formulation of an optimization problem implies the presence of its object, the presence of independent parameters (variables) that describe this problem, as well as conditions (often called restrictions) that characterize the acceptable values of independent variables. An obligatory component of the description of the optimization problem is a scalar measure of "quality", called the criterion of optimality or the objective function, which depends on the optimization variables. The solution of the optimization problem is the search for a certain set of values of variables, which corresponds to the optimal value of the optimality criterion.

When designing a power supply scheme, as a rule, the monetary costs of this scheme are minimized. Reducing power losses due to the installation of compensating devices reduces the costs of the circuit, however, compensating devices also require monetary costs.

METHODS. In this regard, the problem arises of determining the optimal power of compensating devices that meets the minimum of total costs. Such a problem belongs to the problem of unconditional optimization and can be solved, for example, by gradient methods.

Consider such a problem for a radial power supply circuit (Fig. 2.). The power supply has a voltage of U . N consumers with reactive capacities Q_1, Q_2, \dots, Q_n are powered from this source. The active resistances of the lines between the source and consumers are R_1, R_2, \dots, R_n . Each i -th consumer can have a Q_{ki} compensating device installed [1].

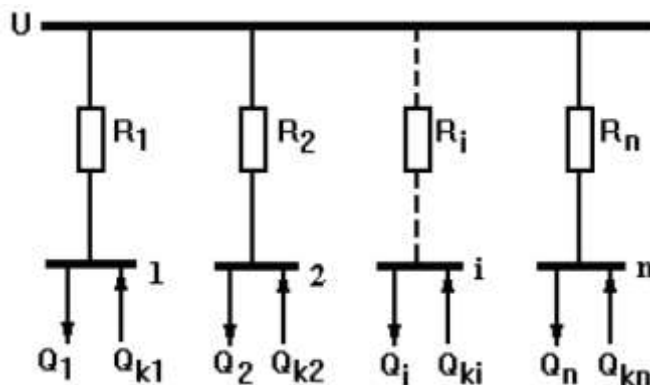


Fig. 2. Radial power supply scheme

It is required to find the optimal distribution between consumers 1, 2, ... n of the given total power of compensating devices Q_k .

The optimality criterion is the minimum loss of active power in the circuit [1, 2, 3].

The objective function to be minimized, which is the loss of active power in the circuit, has the following form [7], [9]:

$$\Delta P = (Q_i - \sum_{k=1}^n Q_k)^2 R_i / U^2 \rightarrow \min. \quad (1)$$

The relative minimum of the objective function is sought under the constraint:

$$Q_{ki} = \sum_{k=1}^n Q_k \quad \text{или} \quad Q_{ki} - \sum_{k=1}^n Q_k = 0. \quad (2)$$

Let's write down the Lagrange function:

$$L = \frac{(Q_i - \sum_{k=1}^n Q_k)^2 R_i}{U^2} + \lambda (\sum_{k=1}^n Q_k - Q_{ki}) \rightarrow \min. \quad (3)$$

To find the minimum of the function L, we calculate its partial derivatives and equate them to zero:

$$\begin{aligned} \frac{dL}{dQ_{k1}} &= -\frac{2R_1(Q_1 - Q_{k1})}{U^2} + \lambda = 0, \\ \frac{dL}{dQ_{k2}} &= -\frac{2R_2(Q_2 - Q_{k2})}{U^2} + \lambda = 0, \end{aligned} \quad (4)$$

$$\begin{aligned} \frac{dL}{dQ_{ki}} &= -\frac{2R_i(Q_i - Q_{ki})}{U^2} + \lambda = 0, \\ \frac{dL}{dQ_{kn}} &= -\frac{2R_n(Q_n - Q_{kn})}{U^2} + \lambda = 0, \end{aligned}$$

$$\frac{dL}{d\lambda} = \sum_{k=1}^n Q_k - Q_{ki} = 0.$$

RESULTS. The analysis of system (4) shows that the optimal distribution of the given total value of the Q_k compensating devices in the radial power supply scheme obeys the equality [6], [8], [10]:

$$R_1 Q_1 - Q_{k1} = R_2 Q_2 - Q_{k2} = \dots = R_i Q_i - Q_{ki} = \dots = R_n Q_n - Q_{kn}. \quad (5)$$

Let's consider the solution of optimization problems in the example of Fig. 2.

The working field for entering initial information is shown in Fig. 1. In cells B2...B10 there is numerical initial information. The desired values of the variables Q_{k1} and Q_{k2} are in cells F1 and F2. The initial values of these variables are assumed to be zero [11], [12].

	A	B	C	D	E	F
1	исходные данные:				переменные	
2	Q1=	600			Qk1=	0,0
3	Q2=	800			Qk2=	0,0
4	R1=	6				
5	R2=	4				
6	U=	10			Целевая функция	
7	z0=	0,5			Z=	1432,0
8	c0=	10				
9	a1=R1*c0*10^-3/U^2=	0,0006				
10	a2=R2*c0*10^-3/U^2=	0,0004				
11						
12	Ограничения:					
13	Qk1>=0					
14	Qk2>=0					
15						

Fig. 1. Initial information of a nonlinear problem on the working field

Table 1
Bringing the coordinate descent with a constant step

Step Number	Q _{k1}	Q _{k2}	Z	Note
At the beginning	0	0	1432	In the direction of Q _{k2} and start the descent
The first step	0	400	864	
The second step	0	800	616	
The third step	0	1200	689	Obviously, it is advisable to stop the descent along the Q _{k2} coordinate, and return to the values of the second step
A new third step	400	800	624	

The solution of this nonlinear problem using Excel software is given [13].

The objective function of fig. 2. using (1) has the form:

$$Z = z_0(Q_{k1} + Q_{k2}) + a_1(Q_1 + Q_2 - Q_{k1} - Q_{k2})^2 + a_2(Q_2 - Q_{k2})^2,$$

where $a_1 = R_1 * c_0 * 10^{-3} / U^2 = 0,0006$, $a_2 = R_2 * c_0 * 10^{-3} / U^2 = 0,0004$.

An expression is entered in cell F7 to calculate the value of this objective function:

$$= B7 * (F2 + F3) + B9 * (B2 + B3 - F2 - F3)^2 + B10 * (B3 - F3)^2.$$

In the dialog box "Search for a solution" (Fig. 2.), the address of the cell of the objective function F7 [4], [5] is set, it is noted that the minimum value of the objective function is being searched; the addresses of cells with the desired variables F2, F3 are indicated; boundary conditions of non-negativity of the desired variables $Q_{k1} \geq 0$ $Q_{k2} \geq 0$ are introduced as constraints.

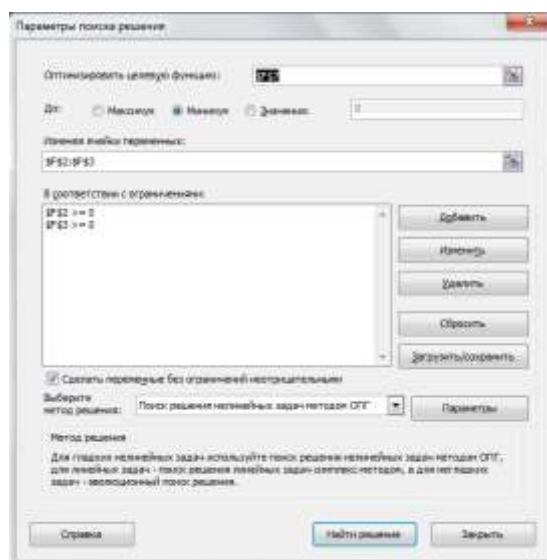


Fig. 2. The "Solution Search" dialog box

CONCLUSION. The results of solving a nonlinear problem, issued by a computer to the working field, are shown in Fig. 3.

The results of the solution are as follows: $Q_{k1} = 183.3$ kVar, $Q_{k2} = 800$ kVar, $Z = 596$ Y.e.

This solution is more accurate, the value of the objective function is 28 y.e. less than in the method of coordinate descent with a constant step.

	A	B	C	D	E	F
1	исходные данные:				переменные	
2	Q1=	600			Qk1=	183,3
3	Q2=	800			Qk2=	800,0
4	R1=	6				
5	R2=	4				
6	U=	10			Целевая функция	
7	z0=	0,5			Z=	595,8
8	c0=	10				
9	$a_1 = R_1 * c_0 * 10^{-3} / U^2 =$	0,0006				
10	$a_2 = R_2 * c_0 * 10^{-3} / U^2 =$	0,0004				
11						
12	Ограничения:					
13	Qk1 >= 0					
14	Qk2 >= 0					
15						

Fig. 3. Results of solving a nonlinear problem on the working field

REFERENCES:

1. Костин В.Н. Оптимизационные задачи электроэнергетики: Учеб.пособие. – СПб.: СЗТУ, 2003 – 120 с.
2. Гайибов Т. Ш. Методы и алгоритмы оптимизации режимов электроэнергетических систем //Т.: Изд. ТашГТУ. – 2014.
3. Насиров Т. Х., Гайибов Т. Ш. Теоретические основы оптимизации режимов энергосистем //Т.:«Fan va texnologiya». – 2014.
4. Кодиров А. А., Комолддинов С. С РЕАКТИВНАЯ МОЩНОСТЬ В ОЦЕНКЕ НАДЕЖНОСТИ ЭНЕРГОСИСТЕМ, ОГРАНИЧЕНИЕ НАГРУЗКИ И КОМПЕНСАЦИЯ// ЭКОНОМИКА И СОЦИУМ. -2022. - №. 5-1 (96). – С. 1124-1130
5. Xakimovich E. A. et al. AUTOMATIC ADJUSTMENT OF VOLTAGE CHANGES USING REACTIVE POWER //Gospodarka i Innowacje. – 2022. – Т. 29. – С. 277-283.
6. Solidjon o'g'li K. S., Abdinabi o'g'li E. H., Axror o'g'li Q. A. Calculation of Power Losses in Electrical Networks Taking into Account Non-Sinusoidal Voltage //Central Asian Journal of Theoretical and Applied Science. – 2022. – Т. 3. – №. 11. – С. 133-144.
7. Kholiddinov I. K. MONITORING QUALITY OF ELECTRIC POWER AT DISTRIBUTION NETWORKS //Central Asian Research Journal for Interdisciplinary Studies (CARJIS). – 2022. – Т. 2. – №. 3. – С. 309-317.
8. Холиддинов И. Х. и др. АНАЛИЗ СНИЖЕНИЯ ПОТЕРЬ В ЭЛЕКТРИЧЕСКИХ СЕТЯХ ПРИ ИСПОЛЬЗОВАНИИ СОВРЕМЕННЫХ ЭЛЕКТРИЧЕСКИХ КАБЕЛЕЙ //Главный редактор: Ахметов Сайранбек Махсутович, д-р техн. наук. – 2022. – С. 26.
9. Xolidinov I. X., Qodirov A. A., Kamoliddinov S. KUCHLANISH O 'ZGARISHINI REAKTIV QUVVATNI AVTOMATIK KOMPENSATSIYALASH QURILMASIDA ROSTLASH //Academic research in educational sciences. – 2022. – Т. 3. – №. 3. – С. 973-981.
10. Пономаренко О. И., Холиддинов И. Х. Автоматизированная система анализа и управления качеством электроэнергии //Главный энергетик. – 2021. – №. 1. – С. 18-24.
11. Khosiljonovich K. I., Ergashevich S. S., Khakimovich E. A. Development of the algorithm of calculation of reactive power by harmonic components //Global Journal of Engineering and Technology Advances. – 2019. – Т. 1. – №. 1. – С. 043-048.
12. Жабборов Т. К., Исмоилов И. К. Анализ проблемы надежности силовых трансформаторов в энергосистемах Республики Узбекистан. – 2021.
13. Hamidjonov Zuhridin, Do'ltayev Ilyosbek SHORT CIRCUIT CHARACTERISTICS IN ELECTRICAL NETWORKS // Universum: технические науки. 2022. №10-7 (103). URL: <https://cyberleninka.ru/article/n/short-circuit-characteristics-in-electrical-networks>.
14. Жабборов Т.К. ДУГОГАСЯЩИЕ РЕАКТОРЫ ДЛЯ КОМПЕНСАЦИИ ЕМКОСТНЫХ ТОКОВ ЗАМЫКАНИЯ НА ЗЕМЛЮ В ПРОМЫШЛЕННЫХ ПРЕДПРИЯТИЯХ // Universum: технические науки : электрон. научн. журн. 2022. 12(105). URL: <https://7universum.com/ru/tech/archive/item/14703>
15. Комолддинов С. С. Ў., Кодиров А. А. Ў. РАЗРАБОТКА СЛОЖНОГО АЛГОРИТМА ЭЛЕКТРИЧЕСКОЙ ЦЕПИ //Universum: технические науки. – 2021. – №. 11-5 (92). – С. 71-75.
16. Khakimovich E. A. et al. Problems of protection during the massive penetration of renewable energy sources in power systems //Наука, техника и образование. – 2019. – №. 10 (63). – С. 26-30.
17. Shestakov A. V. Application of Complete Factorial Experiment to Optimize Parameters of Frequency-Controlled Asynchronous Motor in Order To Improve Its Energy Indicators //2020 International Conference on Industrial Engineering, Applications and Manufacturing (ICIEAM). – IEEE, 2020. – С. 1-5.
18. Hikmatilla Sherzodjon O'G'Li Ne'Matonov MATLAB DASTURIDA ELEKTR ENERGIYA TIZIMIDAGI KATTA TURTKILAR NATIJASIDAGI DINAMIK TURG'UNLIGINIG MATMATIK VA FIZIK MODELLARINING TAHLILI // Scientific progress. 2021. №6. URL: <https://cyberleninka.ru/article/n/matlab-dasturida-elektr-energiya-tizimidagi-katta-turtkilar-natijasidagi-dinamik-turg-unliginig-matmatik-va-fizik-modellarining> (дата обращения: 15.12.2022).
19. Исмоилов И. К., Халилова Ф. А. Регулирование активной и реактивной мощности синхронного генератора при подключении к сети //Universum: технические науки. – 2021. – №. 1-3 (82). – С. 21-25.
20. Zuhridin H. et al. Reactive power compensation in power grids //Universum: технические науки. – 2021. – №. 11-6 (92). – С. 87-90.
21. Kamoliddinov S. et al. РЕГУЛИРОВКА ИЗМЕНЕНИЯ НАПРЯЖЕНИЯ В УСТРОЙСТВЕ АВТОКОМПЕНСАЦИИ (НА ПРИМЕРЕ ОДНОЙ ФАЗЫ) //Главный редактор: Ахметов Сайранбек Махсутович, д-р техн. наук; Заместитель главного редактора: Ахмеднабиев Расул Магомедович, канд. техн. наук; Члены редакционной коллегии. – 2022. – С. 49.
22. Ilkhombek K., Abdvokhid A., Mukhayyo A. ALGORITHM FOR DETERMINING THE NOSINUSOIDALITY COEFFICIENT OF ELECTRICAL QUALITY INDEX FOR WELDING EQUIPMENT //Universum: технические науки. – 2022. – №. 5-12 (98). – С. 29-33.
23. Исмоилов И. К., Турсунов Д. А. ПРИМЕНЕНИЕ МЕТОДОВ РОБАСТНОГО УПРАВЛЕНИЯ В СИСТЕМАХ РЕГУЛИРОВАНИЯ СИНХРОННЫХ ГЕНЕРАТОРОВ //Universum: технические науки. – 2020. – №. 12-5 (81). – С. 28-31.

24. Бойназаров Б. Б. Методы регулировки напряжения //Главный редактор: Ахметов Сайранбек Махсутович, д-р техн. наук. – 2021. – С. 58.
25. Эргашев К. Р. У. РЕГУЛИРОВАНИЕ НАПРЯЖЕНИЯ В ЭЛЕКТРИЧЕСКОЙ СЕТИ //Universum: технические науки. – 2021. – №. 12-6 (93). – С. 46-48.